CHEM 1423 Chapters 18 Homework Solutions

TEXTBOOK HOMEWORK

18.15 Lower $[H^+]$ || higher pH

- (a) $Ka = 4x10^{-5}$: Lower $Ka \parallel lower [H^+]$
- (b) pKa = 3.5: Higher $pKa \parallel lower Ka \parallel lower [H^+]$
- (c) 0.01 M: lower concentration \parallel lower [H⁺]
- (d) Weaker Acid: lower [H⁺]
- (e) 0.01 M Base: Base has lower $[H^+]$
- (f) pOH = 6: Has higher pH (8)

18.16 (a) $[OH^-] = 0.0111 \text{ M} \parallel pOH = -\log(0.0111) = 1.95 \rightarrow pH = 14 - 1.95 \approx 12.05 \text{ Basic}$

(b) $[H^+] = 1.35 \times 10^{-3} \text{ M} \text{ } pH = -\log(1.35 \times 10^{-3}) = 2.87 \rightarrow pOH = 14 - 2.87 \approx 11.13$ Acidic

18.18 (a) $pH = 9.85 \parallel pOH = 14 - 9.85 = 4.15$, $[H^+] = 10^{-pH} = 10^{-9.85} = 1.4 \times 10^{-10} M$ $[OH^-] = 10^{-pOH} = 10^{-4.15} = 7.1 \times 10^{-5} M$

(b) $\text{pOH} = 9.43 \parallel \text{pH} = 14 - 9.43 = 4.57$, $[H^+] = 10^{-pH} = 10^{-4.57} = 2.7 \times 10^{-5} M$ $[\text{OH}^-] = 10^{-pOH} = 10^{-9.43} = 3.7 \times 10^{-10} M$

18.20 Goal: Calculate initial number of moles of H⁺ and final number of moles of H⁺. The difference is the number of moles of OH⁻ which must be added. $[H^+]_{init} = 10^{-pH_{init}} = 10^{-4.52} = 3.020 x 10^{-5} M$ $n[H^+]_{init} = [H^+]_{init} V = 3.020 x 10^{-5} M (5.60 L) = 1.691 x 10^{-4} mol$ $[H^+]_{fin} = 10^{-pH_{fin}} = 10^{-5.25} = 5.623 x 10^{-6} M$ $n[H^+]_{fin} = [H^+]_{fin} V = 5.623 x 10^{-6} M (5.60 L) = 3.15 x 10^{-5} mol$

 $\Delta n[H^+] = n[H^+]_{fin} - n[H^+]_{init} = 3.149 \times 10^{-5} - 1.691 \times 10^{-4} = -1.38 \times 10^{-4} mol$ In order to remove 1.38×10^{-4} moles of H⁺ from the solution, we must **add** 1.38×10^{-4} moles of [OH⁻].

18.45
$$HA \xleftarrow{K_a} H^+ + A^-$$

 $[H^+] = [A^-] = x = 10^{-pH} = 10^{-4.88} = 1.32 \times 10^{-5} \text{ M}, [HA] = 0.035 \text{-}x \approx 0.035$
 $K_a = \frac{[H^+][A^-]}{[HA]} = \frac{(1.32 \times 10^{-5})^2}{0.035} = 4.97 \times 10^{-9} \approx 5.0 \times 10^{-9}$

18.48 pKa = 2.87
$$\parallel K_a = 10^{-pKa} = 10^{-2.87} = 1.35 \times 10^{-3}$$

 $ClCH_2COOH \xleftarrow{K_a} H^+ + ClCH_2COO^-$
[ClCH_2COO⁻] = [H⁺] = x , [ClCH_2COOH] = 1.25 - x ≈ 1.25 M**
 $K_a = 1.35 \times 10^{-3} = \frac{[H^+][ClCH_2COO^-]}{[ClCH_2COOH]} = \frac{x^2}{1.25}$
 $x^2 = 1.35 \times 10^{-3} (1.25) = 1.69 \times 10^{-3} \rightarrow x = 4.11 \times 10^{-2} \approx 0.041 M$
[H⁺] = [ClCH_2COO⁻] = x = 0.041 M , [ClCH_2COOH] = 1.25 - x = 1.21 M ≈ 1.25 M
 $pH = -\log(0.041) \approx 1.4$

18.50
$$HA \xleftarrow{K_a} H^+ + A^- [HA]_o = 0.20 \text{ M}$$
, 3% dissociated
(a) $[\mathbf{H}^+]$, $[\mathbf{OH}^-]$, \mathbf{pH} , \mathbf{pOH}
 $[H^+] = [A^-] = \frac{3}{100} [HA]_o = \frac{3}{100} (0.20 M) = 0.006 M$
 $[HA] = \frac{97}{100} [HA]_o = \frac{97}{100} (0.20 M) = 0.194 M$
 $pH = -\log(0.006) = 2.22$
 $pOH = 14 - 2.22 = 11.78$
 $[OH^-] = 10^{-11.78} = 1.66 x 10^{-12} M \approx 1.7 x 10^{-12} M$
(b) $\mathbf{K}_{\mathbf{a}}$

$$K_a = \frac{[H^+][A^-]}{[HA]} = \frac{(0.006)(0.006)}{0.194} = 1.86x10^{-4} \approx 1.9x10^{-4}$$

18.54 For convenience, let's call HC₉H₇O₄ = HAsp: $HAsp \xleftarrow{K_a} H^+ + Asp^-$, K_a = 3.6x10⁻⁴ [H⁺] = [Asp⁻] = x, [HAsp] = 0.018 - x ≈ 0.018 $K_a = 3.6x10^{-4} = \frac{[H^+][Asp^-]}{[HAsp]} = \frac{x^2}{0.018}$ $x^2 = 3.6x10^{-4} (0.018) = 6.48x10^{-6} \rightarrow x = 2.55x10^{-3} = [H^+]$ $pH = -\log(2.55x10^{-3}) = 2.59 \approx 2.6$ **18.55** Formic Acid: HCOOH. For convenience, we'll call this HForm. $K_a = 1.8 \times 10^{-4}$. This value was looked up in a table. It would be given to you on a test. $HForm \overleftarrow{\longleftarrow} H^+ + Form^ [H^+] = [Form^-] = x$, $[HForm] = 0.75 - x \approx 0.75$ $K_a = 1.8 \times 10^{-4} = \frac{[H^+][Form^-]}{[HForm]} = \frac{x^2}{0.75}$ $x^2 = 1.8 \times 10^{-4} (0.75) = 1.35 \times 10^{-4} \rightarrow x = 1.16 \times 10^{-2} = [Form^-]$ The concentration of the dissociated species is $[Form^-]$. Therefore, the percent dissociation is given by: $\% Dissoc = \frac{[Form^-]}{[HForm]_o} \times 100 = \frac{1.16 \times 10^{-2}}{0.75} \times 1.5\%$

(a) KCN: The salt dissociates completely to K⁺(aq) and CN⁻(aq). KCN J K⁺ + CN⁻(0.15 M). The K⁺ is unimportant because it is the conjugate acid of the infiniely strong base, KOH, and does not react with water. CN⁻ is the conjugate base of the weak acid, HCN, K_a = 6.2x10⁻¹⁰ (Appendix C of the text). You would be given the value on a test. Note: Because you have just put the conjugate base of a weak acid in solution, you know that your solution should have pH > 7. CN⁻ reacts with water according to: CN⁻ + H₂O ← HCN + OH⁻

 $[HCN] = [OH^{-}] = x$, $[CN^{-}] = 0.15 - x \approx 0.15 M$ We get $K_b(CN^+)$ from: $K = 1x10^{-14}$

$$\begin{split} K_a K_b &= K_w \to K_b (CN^-) = \frac{K_w}{K_a (HCN)} = \frac{100}{6.2 \times 10^{-10}} = 1.61 \times 10^{-5} \\ K_b &= \frac{[HCN][OH^-]}{[CN^-]} \to 1.61 \times 10^{-5} = \frac{x \cdot x}{0.15} \\ x^2 &= (0.15)(1.61 \times 10^{-5}) = 2.42 \times 10^{-6} \to x = 1.55 \times 10^{-3} = [OH^-] \\ pOH &= -\log([OH^-] = -\log(1.55 \times 10^{-3}) = 2.81 \\ pH &= 14 - 2.81 = 11.19 \approx 11.2 \end{split}$$

(b) Triethylammonium Chloride, (CH₃CH₂)₃NHCl. Let's call this Et₃NHCl for convenience.

Et₃NHCl \parallel Et₃NH⁺(0.40 M) + Cl⁻. The Cl⁻ is unimportant because it is the conjugate base of the infinitely strong acid, HCl.

 Et_3NH^+ is the conjugate acid of the weak base, Et_3N , $K_b = 5.2 \times 10^{-4}$ (Appendix C of the text). You would be given this value on a test.

Note: Because you have just put the conjugate base of a weak acid in solution, you know that your solution should have pH > 7.

Et₃NH⁺ dissociates according to: $Et_3NH^+ \xleftarrow{K_x} H^+ + Et_3N$ [H⁺] = [Et₃N] = x , [Et₃NH⁺] = 0.40 - x \approx 0.40 We get K_a(Et₃NH⁺) from:

$$K_{a}K_{b} = K_{w} \rightarrow K_{a}(\text{Et}_{3}\text{NH}^{+}) = \frac{K_{w}}{K_{b}(\text{Et}_{3}\text{N})} = \frac{1x10^{-14}}{5.2x10^{-4}} = 1.92x10^{-11}$$
$$K_{a} = \frac{[H^{+}[\text{Et}_{3}N]}{[\text{Et}_{3}\text{NH}^{+}]} \rightarrow 1.92x10^{-11} = \frac{x \cdot x}{0.40}$$
$$x^{2} = (0.40)(1.92x10^{-11}) = 7.69x10^{-12} \rightarrow x = 2.77x10^{-6} = [H^{+}]$$
$$p\text{H} = -\log(2.77 \times 10^{-6}) = 5.56 \approx 5.6$$

18.67 NaClO dissociates completely into Na⁺ + ClO⁻. Because Na⁺ is the conjugate acid of the infinitely strong base, NaOH, it does nothing in solution. On the other hand, ClO⁻ is the conjugate base of the weak acid, HClO. $K_a = 2.9 \times 10^{-8}$ (Appendix C of the text). You would be given this value on a test.

Let's go ahead and get K_b, which we will need in the problem.

$$K_a K_b = K_w \rightarrow K_b (ClO^-) = \frac{K_w}{K_a (HClO)} = \frac{1x10^{-14}}{2.9x10^{-8}} = 3.45x10^{-7}$$

Strategy: (1) We will use the mass percent of NaClO and the density of the solution to calculate the initial concentration, [ClO⁻]. (2) We will use the base equilibrium equation to determine [OH⁻] and pOH/pH.

(1) [CIO⁻] Assume 1.0 L = 1000 mL of solution. Because d = 1 g/mL, we have 1,000 grams. M(NaClO) = 74.5 g/mol. $mass(NaClO) = \frac{6.5}{100} (1,000 g) = 65.0 g$ $n(NaClO) = 65.0 g \cdot \frac{1mol}{74.5 g} = 0.87 mol$

Because NaClO dissociates completely to ClO⁻ (+ Na⁺, which is unimportant), $n(ClO^{-}) = 0.87$ mol. Therefore, $[ClO^{-}]_0 = 0.87$ mol/1.0 L = 0.87 M.

(2) Determine [OH⁻], pOH, pH

ClO⁻ reacts with water according to: $ClO^- + H_2O \xleftarrow{K_b} HClO + OH^-$ [HClO] = [OH⁻] = x , [ClO⁻] = 0.87 - x \approx 0.87 M

$$\begin{split} K_b &= \frac{[HClO][OH^-]}{[ClO^-]} \to 3.45 \times 10^{-7} = \frac{x \cdot x}{0.87} \\ x^2 &= (0.87)(3.45 \times 10^{-7}) = 3.00 \times 10^{-7} \to x = 5.48 \times 10^{-4} = [OH^-] \\ pOH &= -\log([OH^-] = -\log(5.48 \times 10^{-4}) = 3.26 \\ pH &= 14 - 3.26 = 10.74 \approx 10.7 \end{split}$$