

Chp 5

Applications of Clausius-Clapeyron Eqn

(1)

Feb. 21

$$\ln\left(\frac{P_2}{P_1}\right) = -\frac{\Delta_{\text{vap}}H}{R} \left[\frac{1}{T_2} - \frac{1}{T_1}\right]$$

Given  $P_1, T_1, T_2, \Delta_{\text{vap}}H$

$\rightarrow P_2$

Given  $P_1, T_1, P_2, \Delta_{\text{vap}}H$

$\rightarrow T_2$

Given  $P_1, P_2, T_1, T_2 \rightarrow \Delta_{\text{vap}}H$

$$\downarrow \ln\left(\frac{P_2}{P_1}\right) = -\frac{\Delta_{\text{vap}}H}{R} \left[\frac{1}{T_2} - \frac{1}{T_1}\right]$$

$$-R \ln\left(\frac{P_2}{P_1}\right) = \Delta_{\text{vap}}H \left[\frac{1}{T_2} - \frac{1}{T_1}\right]$$

$$\Delta_{\text{vap}}H = \frac{-R \ln\left(\frac{P_2}{P_1}\right)}{\frac{1}{T_2} - \frac{1}{T_1}}$$

The enthalpy of vaporization of toluene is 33.8 kJ/mol.  
The normal boiling point is 111 °C. What is the vapor pressure of toluene, in torr, at 50 °C?

$$\Delta_{\text{vap}}H = 33.8 \text{ kJ/mol} \\ = 3.38 \times 10^4 \text{ J/mol}$$

$$\ln\left(\frac{P_2}{P_1}\right) = -\frac{\Delta_{\text{vap}}H}{R} \left[ \frac{1}{T_2} - \frac{1}{T_1} \right]$$

$$P_1 = 1 \text{ bar} = 1000 \text{ hPa}$$

$$T_1 = 111^\circ\text{C} = 384 \text{ K}$$

$$T_2 = 50^\circ\text{C} = 323 \text{ K}$$

$$P_2 = ?$$

$$\ln\left(\frac{P_2}{1 \text{ bar}}\right) = \frac{-3.38 \times 10^4 \text{ J/mol}}{8.315 \text{ J/mol}\cdot\text{K}} \left[ \frac{1}{323 \text{ K}} - \frac{1}{384 \text{ K}} \right]$$

$$= -2.00$$

$$\ln\left(\frac{P_2}{1 \text{ bar}}\right) = -2.00 \\ \Rightarrow e^{\ln(P_2/1 \text{ bar})} = e^{-2.00}$$

$$\frac{P_2}{1 \text{ bar}} = 0.135$$

$$P_2 = 0.135 \text{ bar} \times \frac{750 \text{ torr}}{1 \text{ bar}}$$

$$= 101 \text{ torr}$$

The enthalpy of vaporization of water is 40.7 kJ/mol.

The normal boiling point is 100 °C.

What is the boiling point of water under a pressure of 2 bar?

$$\Delta_{\text{vap}}H = 40.7 \text{ kJ/mol} \\ = 4.07 \times 10^4 \text{ J/mol}$$

$$T_1 = 100^\circ\text{C} = 373\text{K}$$

$$P_1 = 1 \text{ bar} = 100 \text{ kPa}$$

$$P_2 = 2 \text{ bar}$$

$$T_2 = ?$$

$$\ln\left(\frac{P_2}{P_1}\right) = -\frac{\Delta_{\text{vap}}H}{R} \left[ \frac{1}{T_2} - \frac{1}{T_1} \right]$$

$$-\frac{R}{\Delta_{\text{vap}}H} \ln\left(\frac{P_2}{P_1}\right) = \frac{1}{T_2} - \frac{1}{T_1}$$

$$\frac{1}{T_2} = \frac{1}{T_1} - \frac{R}{\Delta_{\text{vap}}H} \ln\left(\frac{P_2}{P_1}\right)$$

$$= \frac{1}{373\text{K}} - \frac{8.31 \text{ J/(K mol)}}{4.07 \times 10^4 \text{ J/mol}} \ln\left(\frac{2}{1}\right)$$

$$= 2.68 \times 10^{-3} \text{ K}^{-1} - 0.14 \times 10^{-3}$$

$$\frac{1}{T_2} = 2.54 \times 10^{-3} \text{ K}^{-1}$$

$$T_2 = \frac{1}{2.54 \times 10^{-3} \text{ K}^{-1}}$$

$$T_2 = 394\text{K} - 273\text{K}$$

$$= 121^\circ\text{C}$$