## Chapter 4 - Homework

4.1 Suppose you put a cube of ice of mass 100 g into a glass of water at $0^{\circ} \mathrm{C}$. When the ice melts, 33 . kJ of energy is absorbed from the surroundings as heat. What is the change of entrop of:
(a) the sample (the ice)
(b) the surroundings (the glass of water)
4.2 A sample of aluminum [ $\mathrm{M}=27$ ] of mass 1.25 kg is cooled at constant pressure from $27^{\circ} \mathrm{C}$ to $-13^{\circ} \mathrm{C}$. Calculate the energy which must be removed as heat and the change in entropy of the sample. Note: The constant pressure molar heat capacity of aluminum is $24.35 \mathrm{~J} / \mathrm{mol}-\mathrm{K}$
4.3 A sample of $\mathrm{CO}_{2}(\mathrm{~g})[\mathrm{M}=44]$ occupies $15 . \mathrm{L}$ at $-23^{\circ} \mathrm{C}$ and 1.00 atm is compressed isothermally. To what volume must the gas be compressed to reduce its entropy by $10.0 \mathrm{~J} / \mathrm{K}$ ?
4.4 Whenever a gas expands, the gas undergoes an increase in entropy. A sample of $\mathrm{CH}_{4}(\mathrm{~g})[\mathrm{M}=16]$ of mass $25 . \mathrm{g}$ at $-23^{\circ} \mathrm{C}$ and 185 kPa expands isothermally until the pressure is 2.5 kPa .
Calculate the entropy change when the gas expands (a) reversibly, (b) irreversibly.
4.5 Calculate the change in molar entropy when an 80 g sample of $\operatorname{argon}[\mathrm{M}=40]$ is compressed from 2.0 L to $500 \mathrm{~cm}^{3}$ and simultaneously heated from 300 K to 400 K .
Note: The constant volume molar heat capacity is $\mathrm{C}_{\mathrm{v}, \mathrm{m}}=12.5$ J/mol
4.6 The enthalpy of vaporizaton of trichloromethane, $\mathrm{CHCl}_{3}$, is 29.4 $\mathrm{kJ} / \mathrm{mol}$ at its normal boiling point, $62^{\circ} \mathrm{C}$.
(a) Calculate the entropy of vaporization of trichloromethane at its normal boiling point.
(b) What is the entropy change of the surroundings?
4.7 Calculate the standard reaction entropy (at 298 K ) of the following two reactions:
(a) $2 \mathrm{CH}_{3} \mathrm{CHO}(\mathrm{g})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{CH}_{3} \mathrm{COOH}(\mathrm{l})$
(b) $2 \mathrm{AgCl}(\mathrm{s})+\mathrm{Br}_{2}(\mathrm{I}) \rightarrow 2 \mathrm{AgBr}(\mathrm{s})+\mathrm{Cl}_{2}(\mathrm{~g})$

## Molar Entropies

| Compound | $\mathbf{S}^{0}$ |
| :--- | :--- |
| $\mathrm{CH}_{3} \mathrm{CHO}(\mathrm{g})$ | $250.3 \mathrm{~J} / \mathrm{mol}-\mathrm{K}$ |
| $\mathrm{O}_{2}(\mathrm{~g})$ | 205.1 |
| $\mathrm{CH}_{3} \mathrm{COOH}$ | 159.8 |
| $\mathrm{AgCl}^{2}(\mathrm{~s})$ | 96.2 |
| $\mathrm{Br}_{2}(\mathrm{l})$ | 152.2 |
| $\mathrm{AgBr}(\mathrm{s})$ | 107.1 |
| $\mathrm{Cl}_{2}(\mathrm{~g})$ | 223.1 |

4.8 A quantity of 0.35 moles of a Perfect Gas at $16^{\circ} \mathrm{C}$ is expanded from 1.2 L to 7.4 L . Calculate $\mathrm{w}, \mathrm{q}, \Delta \mathrm{U}, \Delta \mathrm{H}, \Delta \mathrm{S}$ and $\Delta \mathrm{G}$ if the process is carried out: (a) isothermally and reversibly, and (b) isothermally and irreversibly against an external pressure of 1.0 bar.
4.9 Calculate $\Delta \mathrm{H}, \Delta \mathrm{U}$ and $\Delta \mathrm{S}$ when 1 mol of water undergoes the following process:

$$
\mathrm{H}_{2} \mathrm{O}\left(\text { liq, } 25^{\circ} \mathrm{C}\right) \rightarrow \mathrm{H}_{2} \mathrm{O}\left(\text { gas, } 100^{\circ} \mathrm{C}\right)
$$

The molar heat of vaporization of water at $100^{\circ} \mathrm{C}$ is $40.7 \mathrm{~kJ} / \mathrm{mol}$. The constant pressure molar heat capacity of water is $75.3 \mathrm{~J} / \mathrm{mol}-\mathrm{K}$
4.10 Use the data below to calculate $\Delta \mathrm{G}^{0}$ for the following reaction:

$$
\beta \text {-D-Glucose(s) }\left[\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(\mathrm{~s})\right] \rightarrow 2 \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(\mathrm{I})+2 \mathrm{CO}_{2}(\mathrm{~g})
$$

using: (a) Enthalpies of formation and standard entropies, and (b) Gibbs energies of formation.

| Compound | $\Delta_{\mathbf{f}} \mathbf{H}^{\mathbf{o}}$ | $\mathbf{S}^{\mathbf{o}}$ | $\Delta_{\mathbf{G}} \mathbf{G}^{\mathbf{o}}$ |
| :--- | :---: | :---: | :---: |
| $\beta$-D-Glucose(s) | $-1268.0 \mathrm{~kJ} / \mathrm{mol}$ | $212.0 \mathrm{~J} / \mathrm{mol}-\mathrm{K}$ | $-910.0 \mathrm{~kJ} / \mathrm{mol}$ |
| $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(\mathrm{I})$ | -277.7 | 160.7 | -174.8 |
| $\mathrm{CO}_{2}(\mathrm{~g})$ | -393.5 | 213.7 | -394.4 |

4.11 As an approximation, one may assume that proteins exist in either the native or denatured state. The standard molar enthalpy and entropy for the denaturation of a certain protein are $512 \mathrm{~kJ} / \mathrm{mol}$ and $1600 \mathrm{~J} / \mathrm{mol}-\mathrm{K}$. At what temperature does the denaturation of this protein become spontaneous? Is the reaction spontaneous at temperatures above OR below this temperature?
4.12 The Enthalpy of Fusion of Benzene is $9.87 \mathrm{~kJ} / \mathrm{mol}$. The Entropy of Fusion of Benzene is $35.4 \mathrm{~J} / \mathrm{mol}-\mathrm{K}$ The normal melting point of benzene is $6^{\circ} \mathrm{C}$.
Calculate $\Delta \mathrm{G}$ for the melting of two moles of benzene at:
(a) $-25^{\circ} \mathrm{C}$, (b) $6{ }^{\circ} \mathrm{C}$, (c) $25^{\circ} \mathrm{C}$

In each case, indicate whether the process is spontaneous, non-spontaneous, at equilibrium.

